



Mathematical methods for productivity and quality in the production of plastic films

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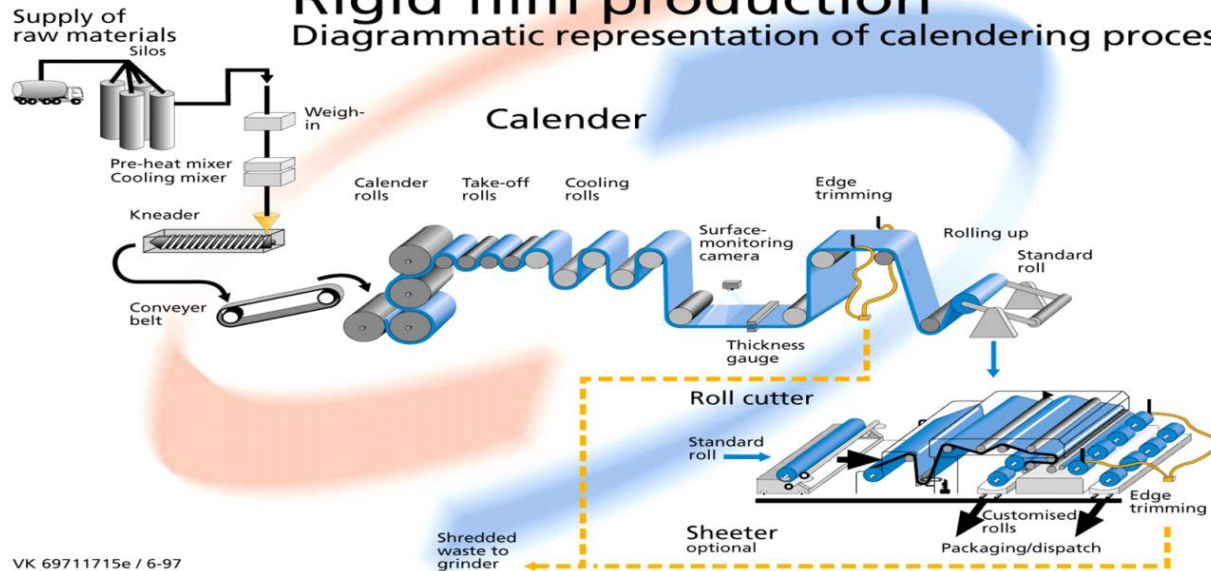


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Mathematical methods for productivity and quality in the production of polymeric films

Film production with calendaring

Rigid film production Diagrammatic representation of calendaring process



VK 69711715e / 6-97

Properties/ quality of kp-films from rigid PVC

- Thickness tolerance MDO, TDO
- Shrink MDO, TDO
- Mistake-free (black points, specks, ...)
- Surface roughness, luster
- Barrier against water vapor and/or oxygen
- Thermoforming
- Printability
- Color consistency
- Mechanical and thermal properties

Kp-machinery

41 calender and calandrette in 9 sites with a capacity of rigid PVC of about 400 Tto/year

Technology

- Silo storage and Big-Bag
- Dosing
- Mixing (heat and cool)
- Gelation (Buss-kneader, extrusion)
- Important roll temperature, roll velocity
roll diameter, surface, roughness
roll parallelism
- Inline measurement
thickness, surface defects, color, gloss

Specification

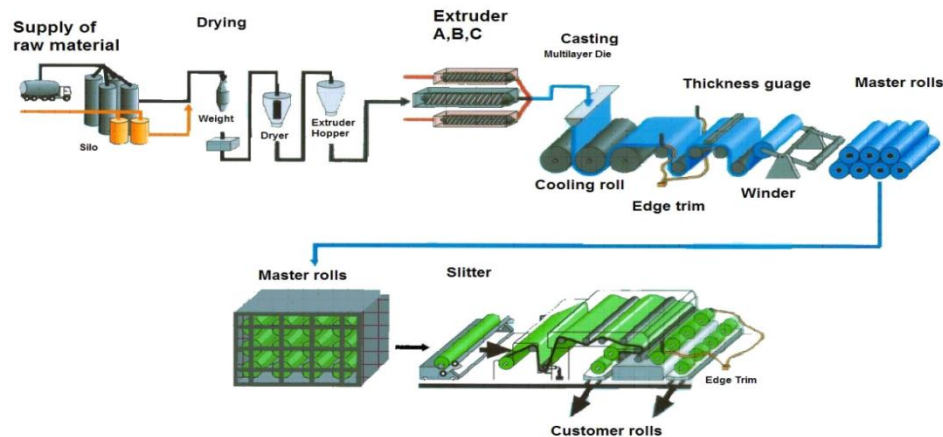
- Thickness from 25 to 1200 μm
- Width from 100 to 2500 mm
- Surface: gloss or different embossed
- Shrinkage from 0 to 60 % MDO
- Color : all Lab

Film production with cast extrusion

Schemata

Extrusion process

Diagrammatic representation of Extrusion process



Properties/ quality of kp-films from extrusion

- Multilayer:
 - Coextrusion, up to 7 layers; multiple polymer combinations
 - Lamination, thermal and aqueous; multiple polymer combinations
 - Side-by-side (XY) structures
- In line MDO or TDO for shrink applications
- Foaming
- PCR-content
- FDA, Reach compliance
- Colors, tints, color consistency, bi-color, light blocking, UV inhibitors
- Surface roughness, luster
- Corona treatment

Kp-machinery

- Global presence, with 35 extrusion lines in 12 sites (Americas, Europe, Asia).
- Global Capacity of over 250ktons/year

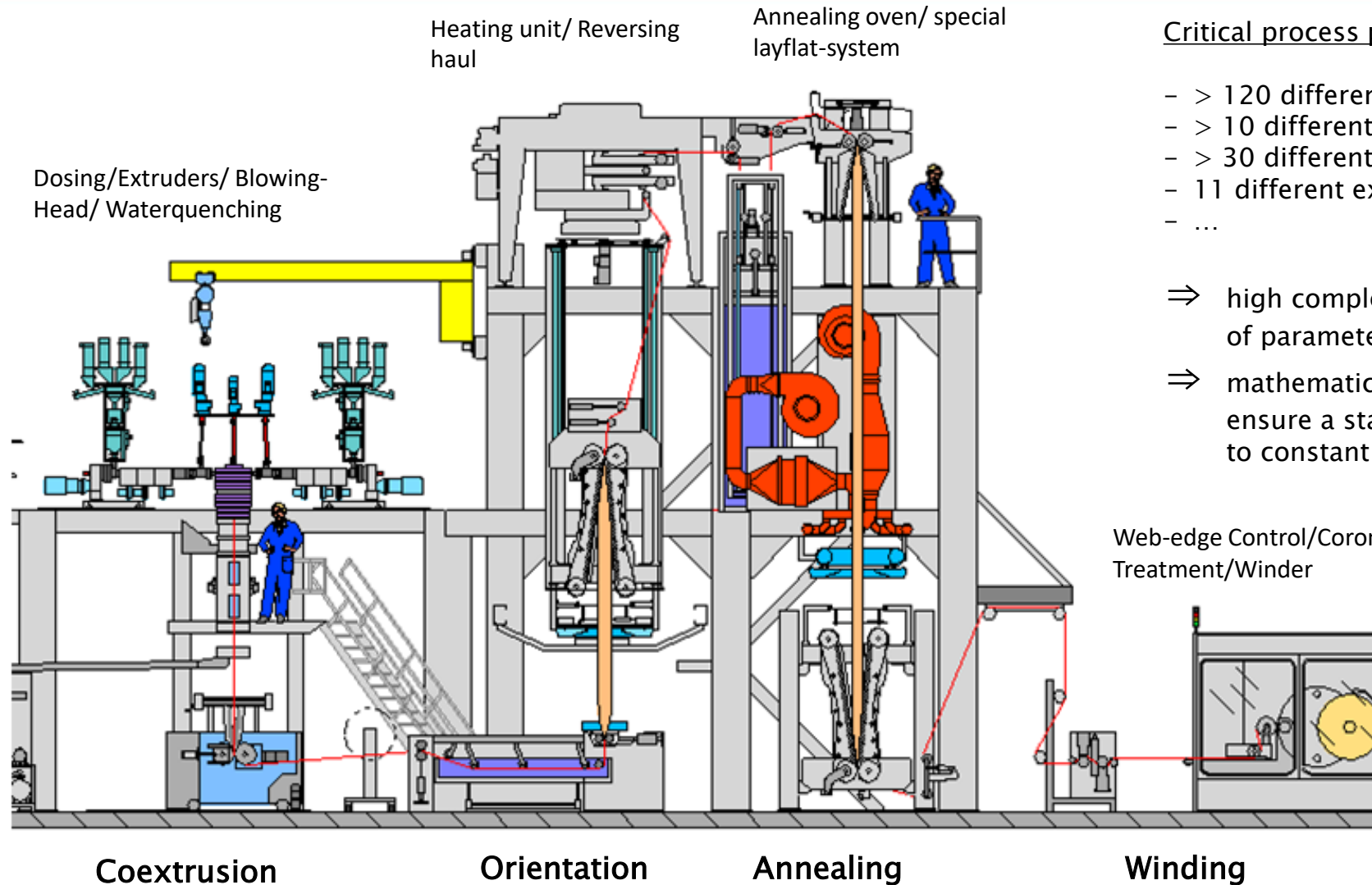
Technology

- Incoming raw materials, drying, blending
- Extrusion, decontamination, melt filtration, foam incorporation
- Layer combination, profile control
- Blown film, cast film, rollstack
- Lamination, Coating, Winding
- In-Line Measurement
 - Vision System (OCS)
 - iV
 - Color, gloss, haze
 - Gauge

Specification

- Thickness from 20 to 1650 μm
- Width up to 2200mm (6.2m for TDO)
- Recycle content up to 100%
- Shrinkage from 0 to 80%, MDO or TDO
- Color tolerance

Film production with blowing extrusion



Critical process parameters:

- > 120 different temperatures
- > 10 different velocities
- > 30 different pressure values
- 11 different extruder output
- ...

⇒ high complexity of the interplay of parameters

⇒ mathematical methods to ensure a stable process leading to constant product quality

Material- and process values in film production

Material value

- Density ρ
- Viscosity $\eta = f(T, \dot{\gamma})$
- Flow index n
- Specific heat capacity c_p
- Heat conduction λ
- Heat transfer k
- Grain size distribution Δd
- Melting temperature T_s



Machine value

- Construction of calender or extrusion
- Construction of nozzle
- Roll diameter D
- Distance h
- Roughness R_z



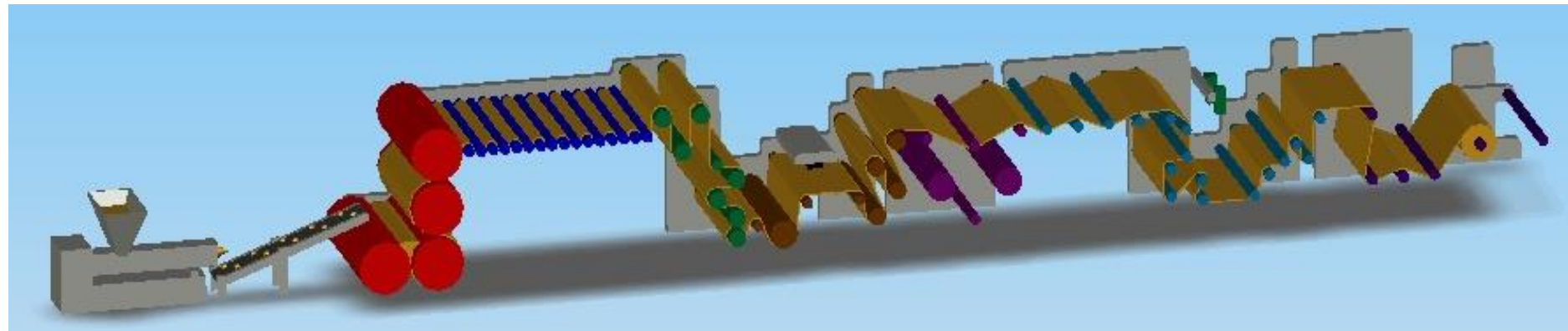
Process value

- Velocity v
- Different velocity Δv
- Temperature T
- Temperature field $T(x,y)$
- Output Q
- Pressure p



Quality value

- Thickness
- Glos
- Color Lab
- Mistake
- Shrinkage
- strength



By calendering : about 100 values with 800 relationship
 example: higher temperature \rightarrow lower viscosity \rightarrow lower pressure \rightarrow higher output
 with lower thickness

Development objectives of Klöckner Pentaplast for calendering film

- High quality (low thickness distribution, no surface defects such as black spots, specks and holes, small color tolerances, optimal shrinkage)
- High productivity (quick changeovers, high velocity, high degree of automation)
- New characteristics for customers and service

Quality of the final product will depend on (cooperation with Prof.Chistyakova)

1. optimal gelling in the extruder
2. Optimal dosing of liquid colors in the extruder
3. optimal thickness distribution by roll-bending and Acrossing
4. optimal cooling of the film for high transparency
5. Optimal shrinkage of polymeric films
6. Small number of films errors

Special characteristics of polymeric films

7. Anticounterfeiting
8. Thermoforming process
9. Ecological properties of different polymeric films
10. Plant development

Basic equations for process optimization

Equation of the conservation of mass

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x}(\rho v_x) + \frac{\partial}{\partial y}(\rho v_y) + \frac{\partial}{\partial z}(\rho v_z) = 0$$

Equation of motion

Die Bewegungsgleichung in kartesischen Koordinaten:

$$\frac{\partial P}{\partial x} = \frac{\partial p_{xx}}{\partial x} + \frac{\partial p_{yx}}{\partial y} + \frac{\partial p_{zx}}{\partial z} - \rho \left(\frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \right)$$

Heat balance

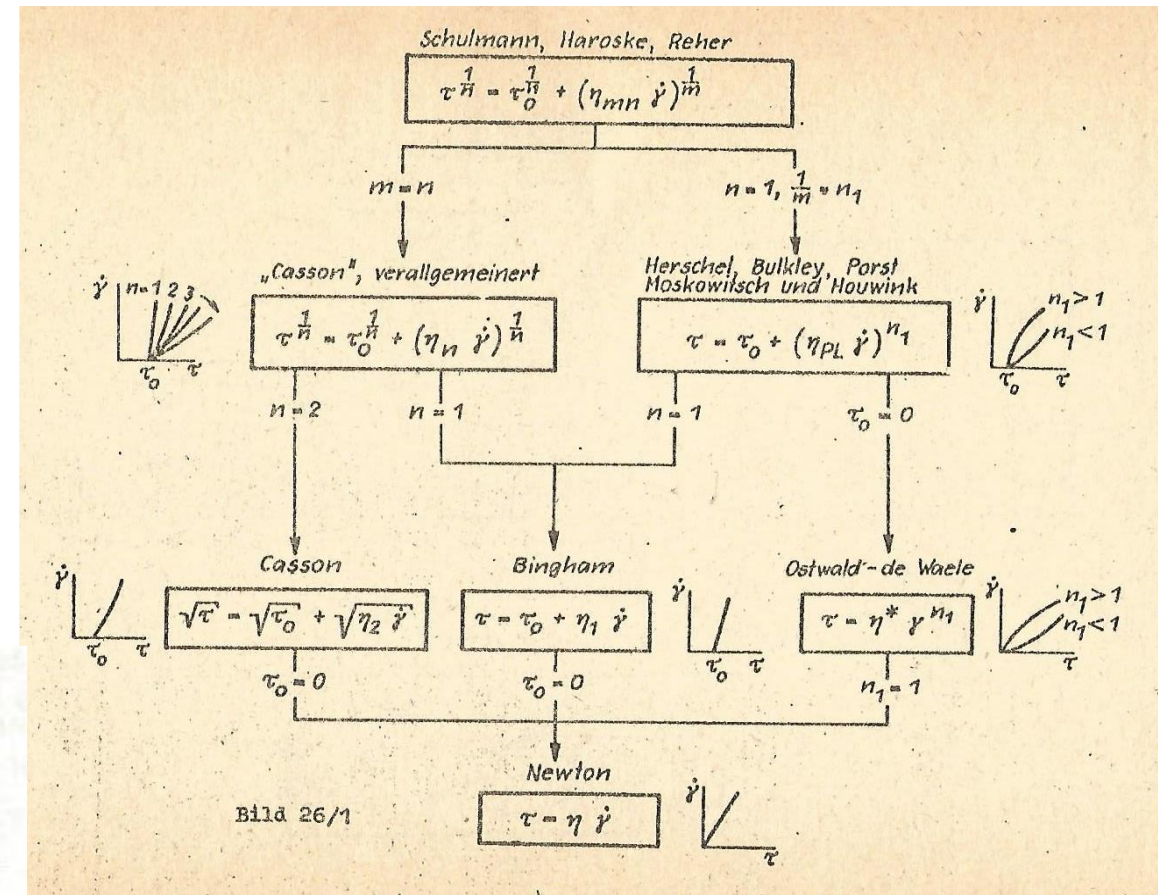
$$\rho c_v \frac{dT}{dt} = -(\nabla \cdot q) - T \left(\frac{\partial P}{\partial T} \right)_\rho (\nabla \cdot v) + (p : \nabla \cdot v)$$

c_v spezifische Wärme bei konstantem Volumen

q Vektor des Wärmestromes

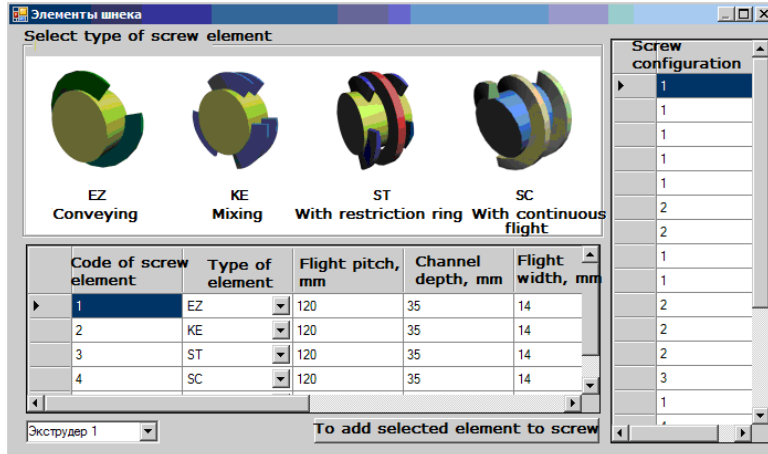
$$q = -k \nabla T$$

k Wärmeleitfähigkeit der Flüssigkeit



rheological state function

1. optimal gelling in the extruder



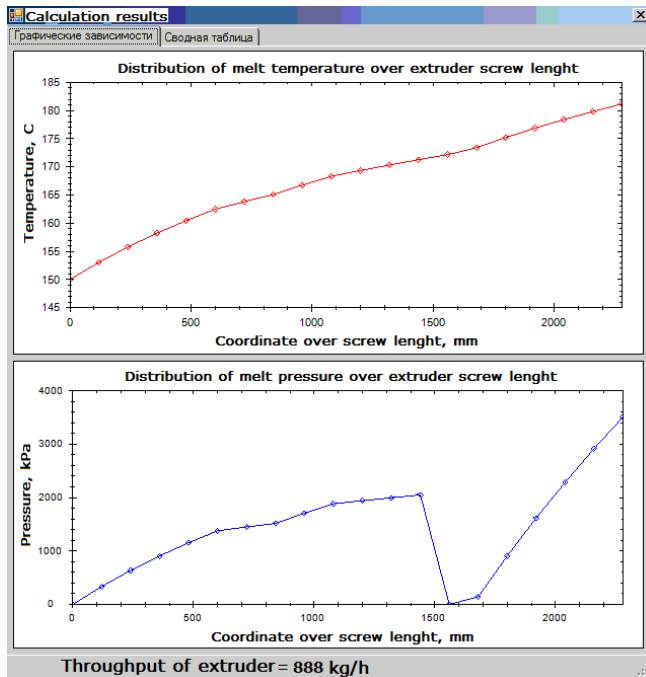
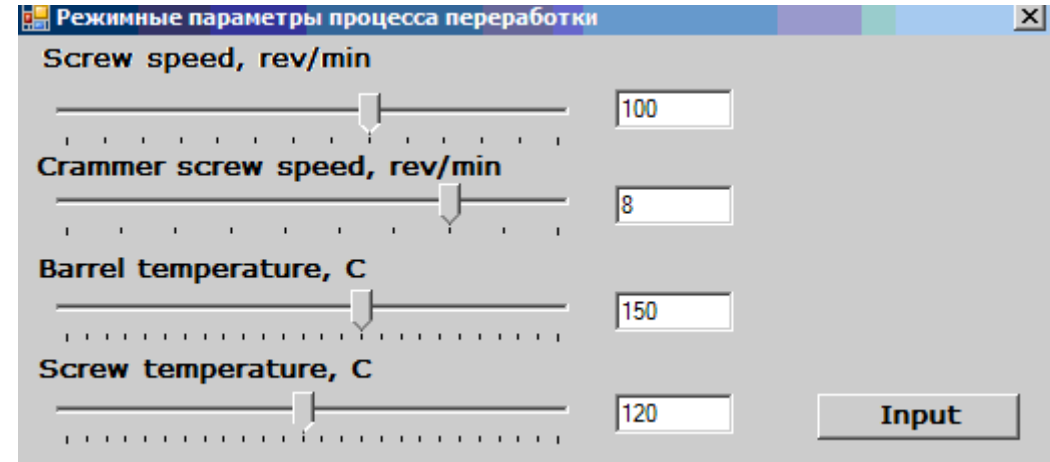
$$\int_0^{H^j} v_x^j dy = \dot{Q}_\delta^j + \dot{Q}_s^j, \quad W^j \cdot \int_0^{H^j} v_z^j dy = Q,$$

$$\partial P^j / \partial x = \partial \tau_{xy}^j / \partial y, \quad \partial P^j / \partial z = \partial \tau_{zy}^j / \partial y,$$

$$\tau_{xy}^j = \eta^j \cdot (dv_x^j / dy), \quad \tau_{zy}^j = \eta^j \cdot (dv_z^j / dy),$$

$$\mu^j = \mu_0 \cdot \exp[-b \cdot (T^j - T_0)],$$

$$\eta^j = \mu^j \cdot \left[(dv_x^j / dy)^2 + (dv_z^j / dy)^2 \right]^{(n-1)/2},$$



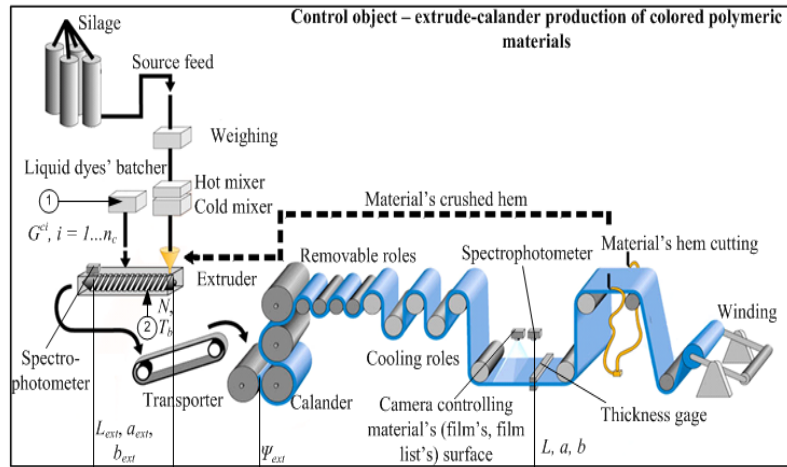
$$\rho \cdot c_p \cdot Q \cdot dT^j / dz = -W^j \cdot [\alpha_b \cdot (T^j - T_b) + \alpha_{scr} \cdot (T^j - T_{scr})] + W^j \cdot (U_x \cdot \tau_{xb}^j + U_z \cdot \tau_{zb}^j) - W^j \cdot (\dot{Q}_\delta^j + \dot{Q}_s^j) \cdot \partial P^j / \partial x - Q \cdot \partial P^j / \partial z,$$

Advantage:

- Control of the entire calender line over kneader
- faster changeover times by prediction

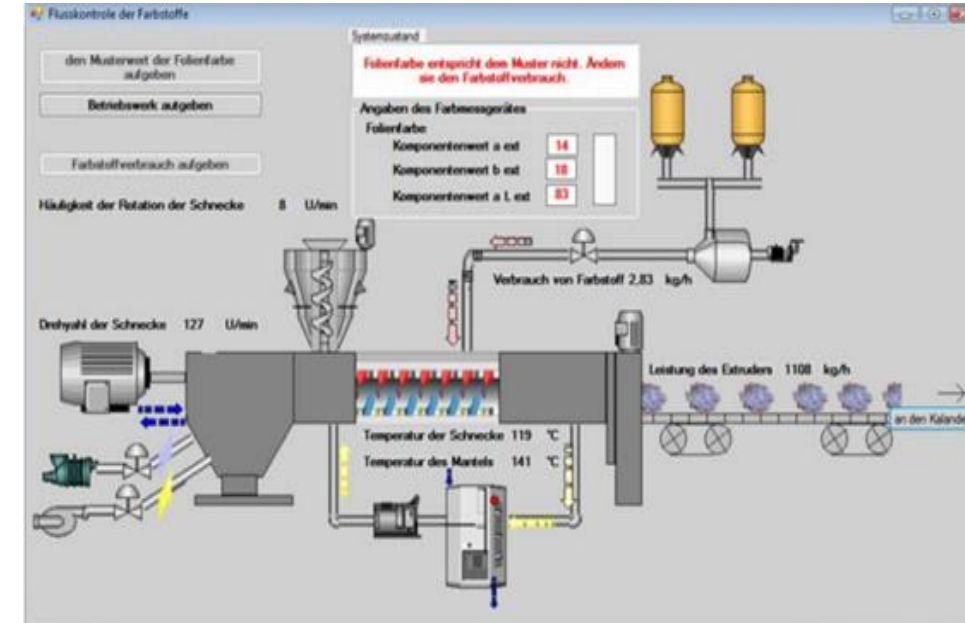


2. Optimal dosing of liquid colors in the extruder



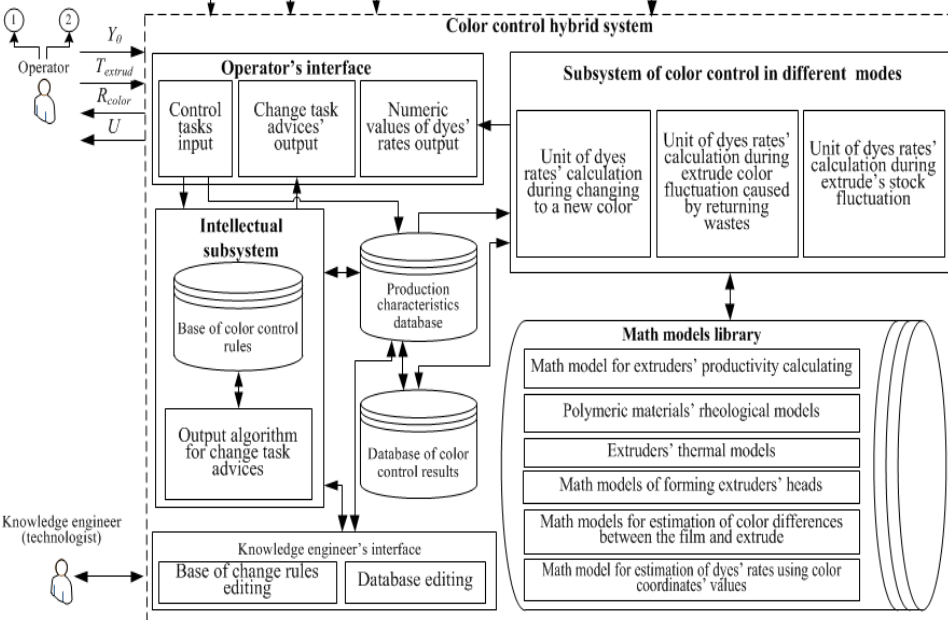
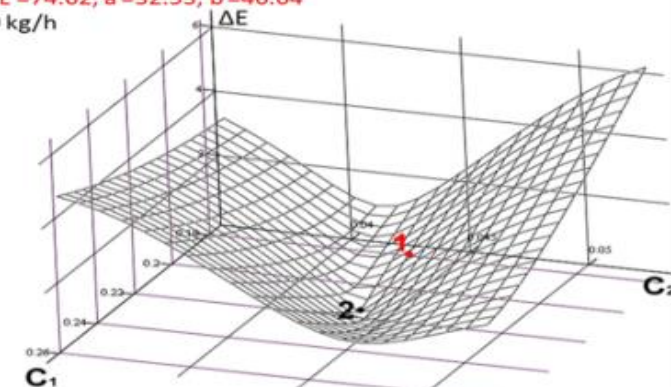
Advantage:

- Reduce color change time from 20 – 30 min to 3-4 min
- rapid correction possibility in color variations $dE < 0,5$



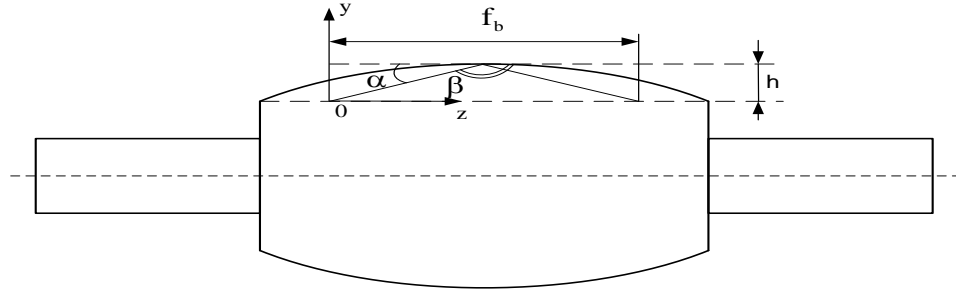
Input data's for testing:
 Standard: $L^* = 74.66, a^* = 32.32, b^* = 48.01, C_1^* = 0.22\%, C_2^* = 0.044\%$
 Current color of a film: $L = 74.62, a = 32.53, b = 46.64$
 Productivities : $G = 1000 \text{ kg/h}$

$\Delta E = 1.391,$
 $C_1 = 0.2\%, C_2 = 0.045\%$
 $\Delta G_1 = 20 \text{ kg/h}$
 $\Delta G_2 = - 1 \text{ kg/h}$



3. Optimal thickness distribution by roll-bending and acrossing

❖ mathematical model of the bompage



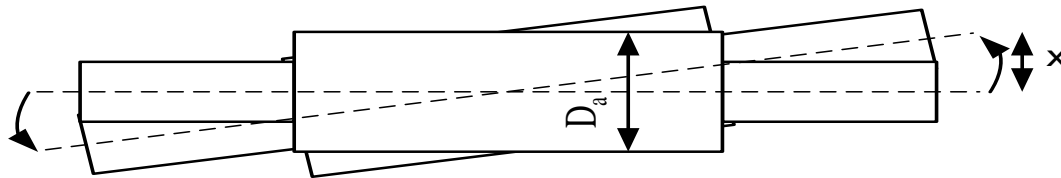
Thickness profil for film

$$S_h(z, h) = \frac{h}{1 - \sin \alpha} \cdot \left\{ \sin \left[\alpha + \frac{\beta - \alpha}{w} \cdot \left(z + \frac{w - f_b}{2} \right) \right] - \sin \alpha \right\}$$

Start and end of the bending

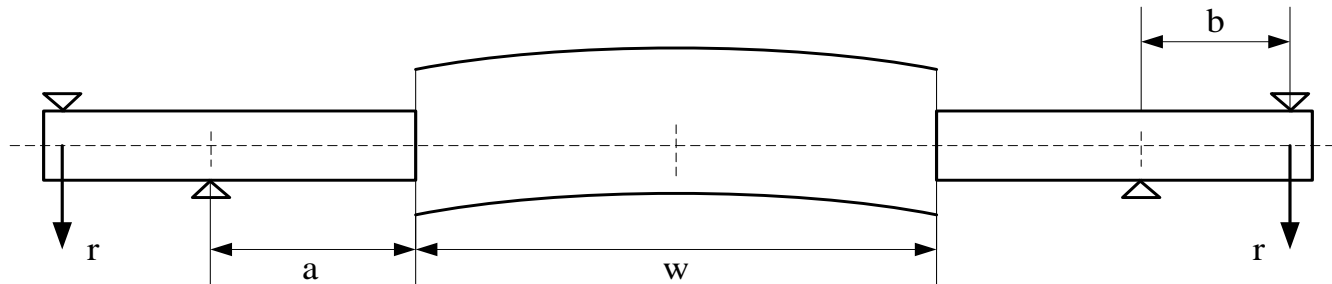
$$\alpha = \frac{\pi}{180} \cdot 20 + \frac{7}{18} \cdot \pi \cdot \frac{(w - f_b)}{w}, \quad \beta = \frac{\pi}{180} \cdot 160 - \frac{7}{18} \cdot \pi \cdot \frac{(w - f_b)}{w}$$

❖ mathematical model of accrossing



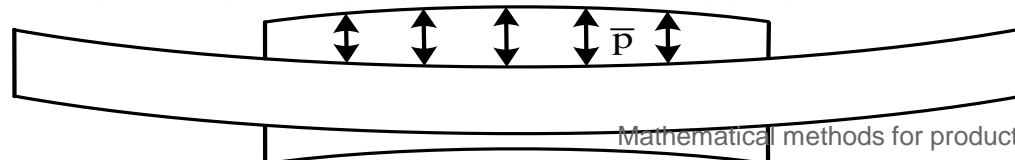
$$S_x(z, x) = \left(\sqrt{\left(x \cdot \frac{f_b}{w} \right)^2 + D_a^2} - D_a \right) \cdot \left(1 - \frac{2 \cdot z}{f_b} \right)^2$$

❖ mathematical model of roll bending



$$S_r(z, r) = \frac{r \cdot b}{2 \cdot E \cdot I_e} \cdot \left[z_3^2 - w \cdot z_3 - a \cdot \left(w + \frac{I_e}{I_w} \cdot a \right) \right]$$

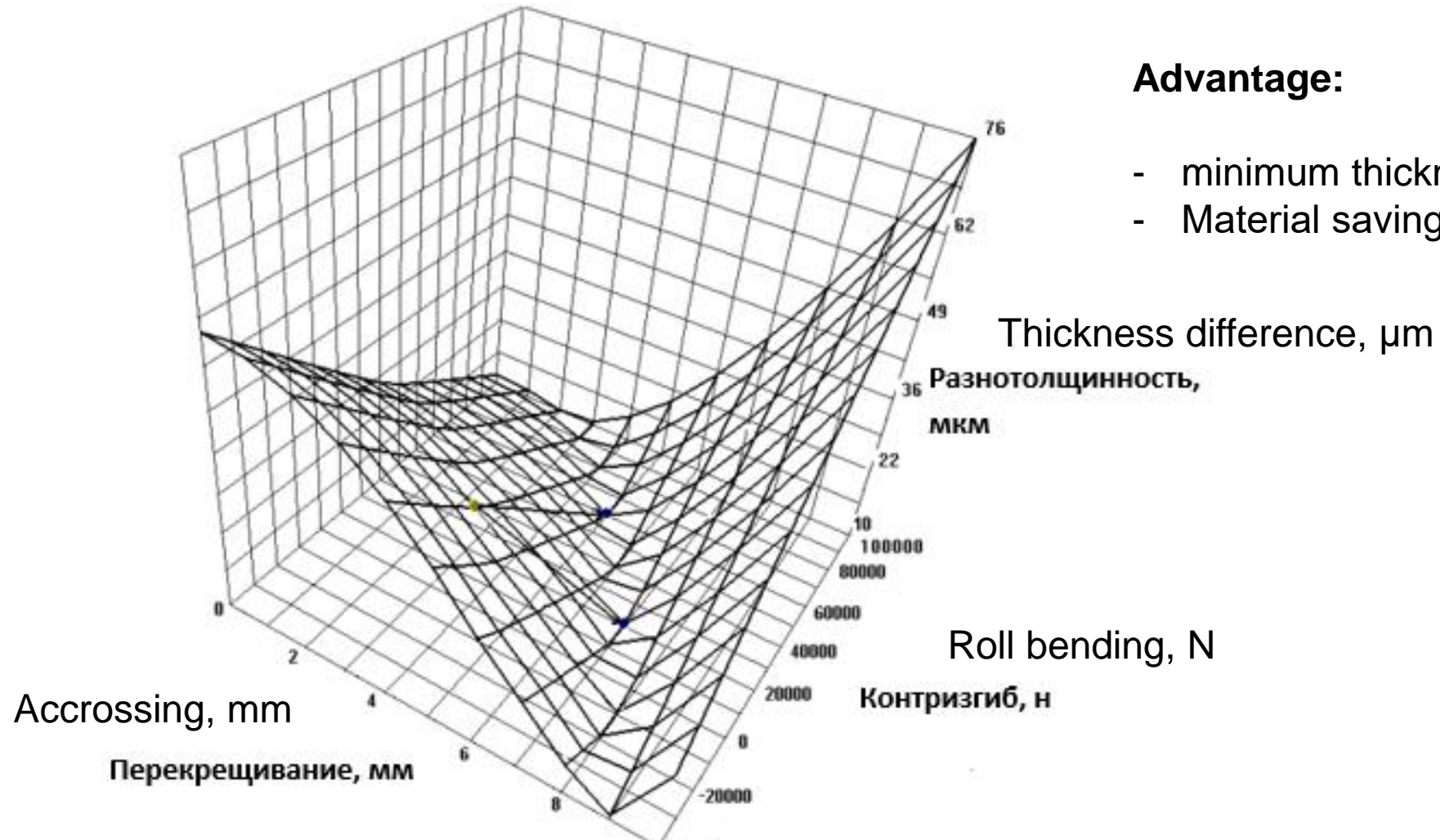
❖ mathematical model of roll deflection



$$S_p(z) = d_2 \cdot z^4 + d_1 \cdot z + d_0, \quad d_k = f_k[S(z), p], \quad k = 0, 1, 2$$

3. Optimal thickness distribution by roll-bending and accrossing

Depending on the film thickness difference of roll bending and accrossing to minimize the difference

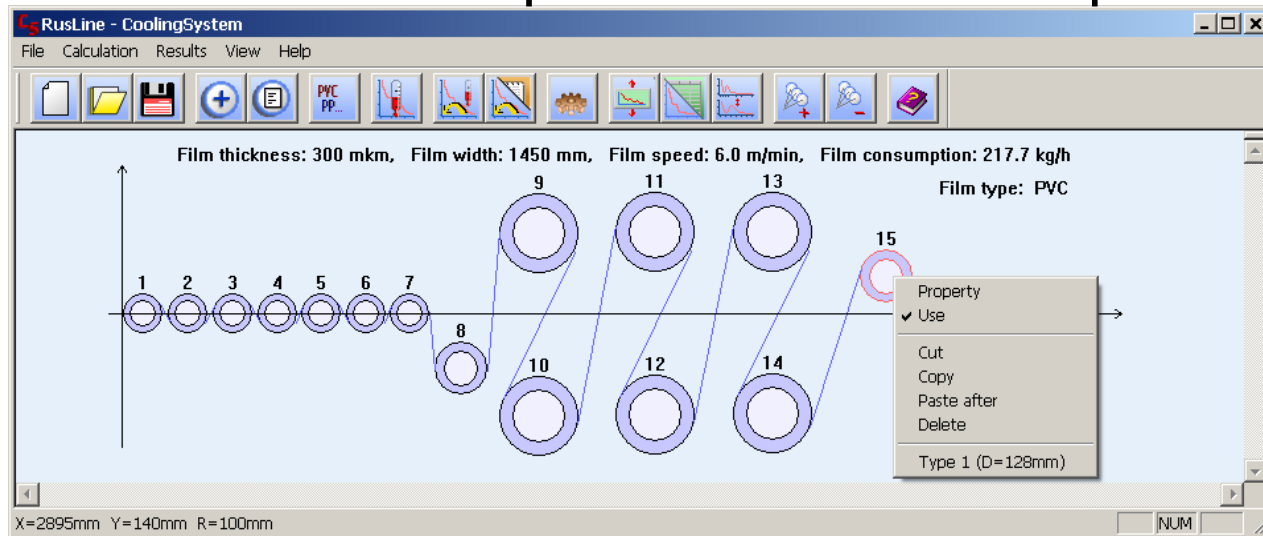


Advantage:

- minimum thickness variations
- Material savings in m² - sale

4. optimal cooling of the film for high transparency

Prediction of the optimum uniform temperature cooling for a high film transparent

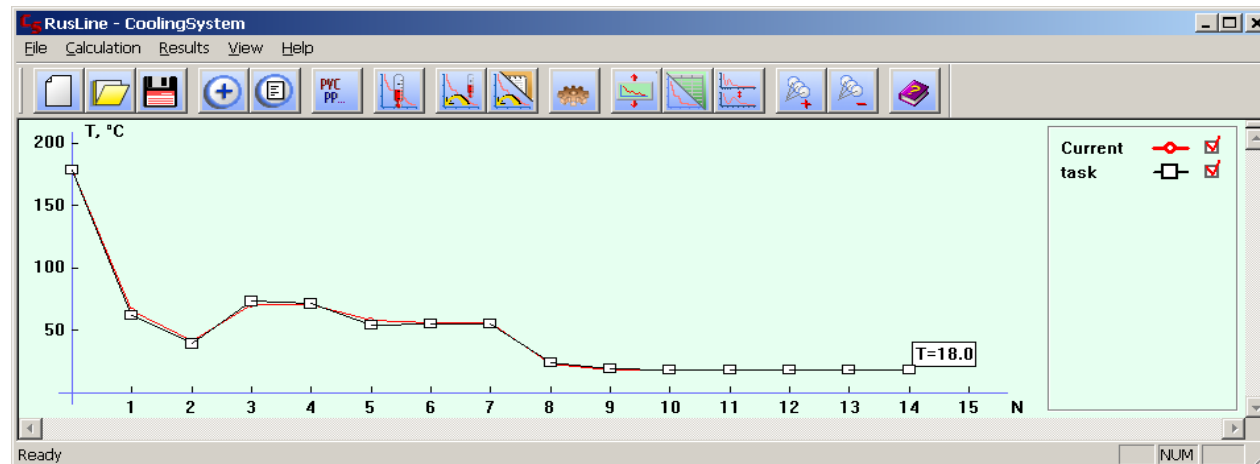


Temperature control is critical for transparency, the film shrinkage and the gloss of the film surface - crucial quality criteria.

The model allows the prediction of the optimum rolling temperatures.

Advantage:

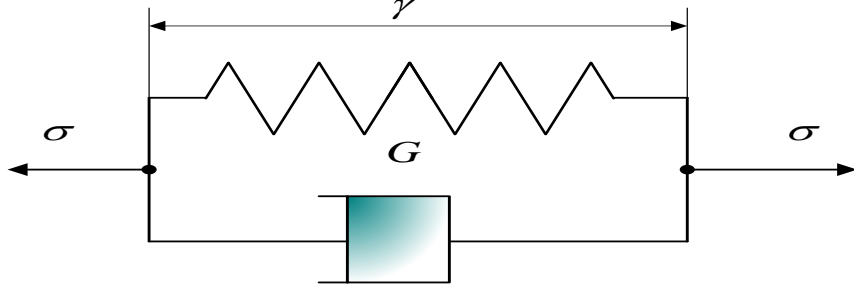
- Reduce of change time
- Reduce complaint for false shrink, gloss or transparency



5. Optimal shrinkage of polymeric films

Modell Muni-Rivlin

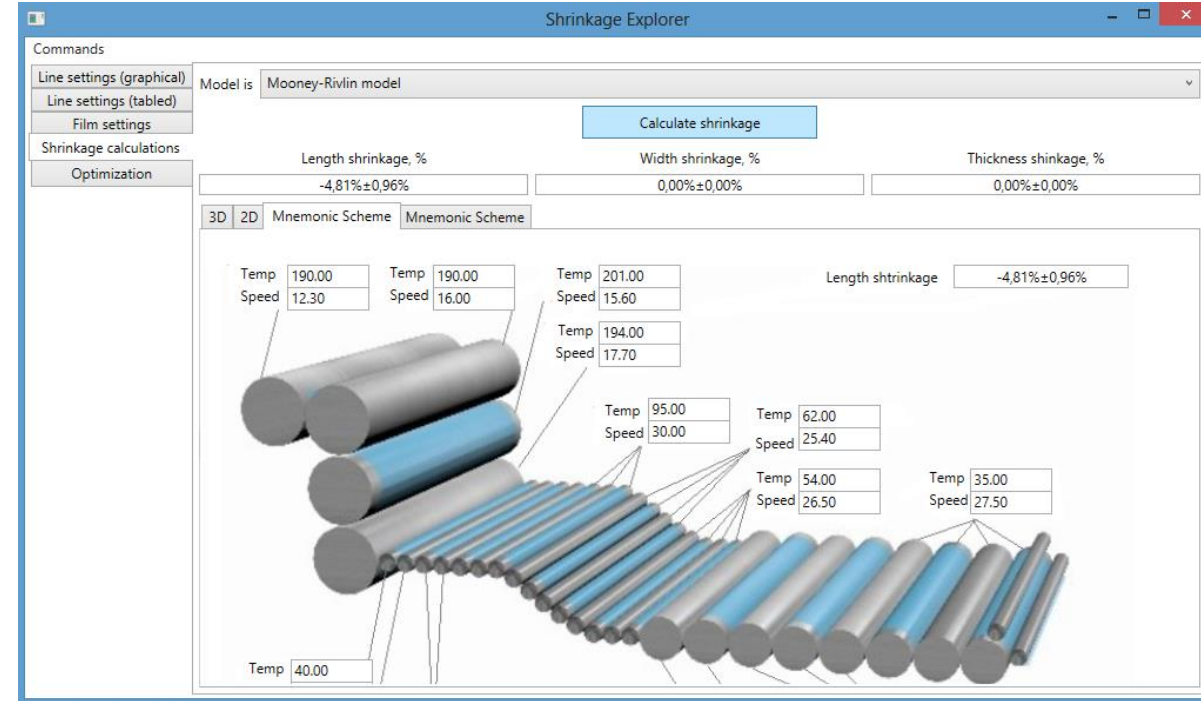
- based on two effects:



- Equation for the shrink between $i-1$ and i roll:

$$C \cdot S_l^6 + A \cdot S_l^4 + \left(B - C - 2^{n+1} \left(\frac{U_{i-1} \cdot n}{L(1-n)} \right)^n \cdot \left[1 - \frac{U_{i-1}}{U_i} \right]^{1-n} \cdot \frac{H_{i-1} W_{i-1}}{HW} \mu_0 e^{-b(T_{i+1} - T_i)} \right) \cdot S_l^3 - A \cdot S_l^2 - B = 0$$

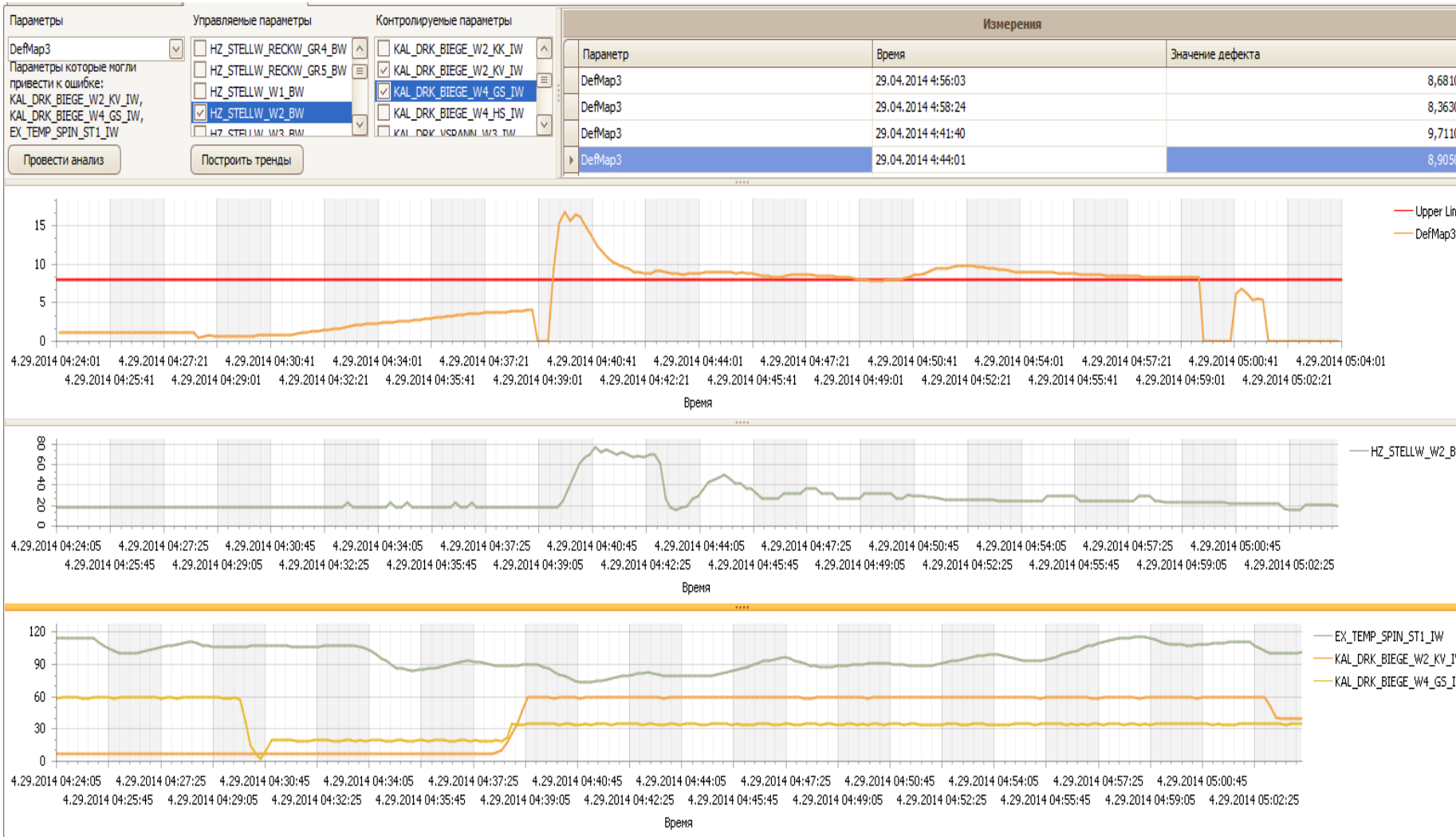
- Total shrinkage is calculated from the sum of the orientations between the rollers of a calender line



Advantage:

- Reducing changeover time
- Reduce of Complaint for false shrink

6. small number of films errors

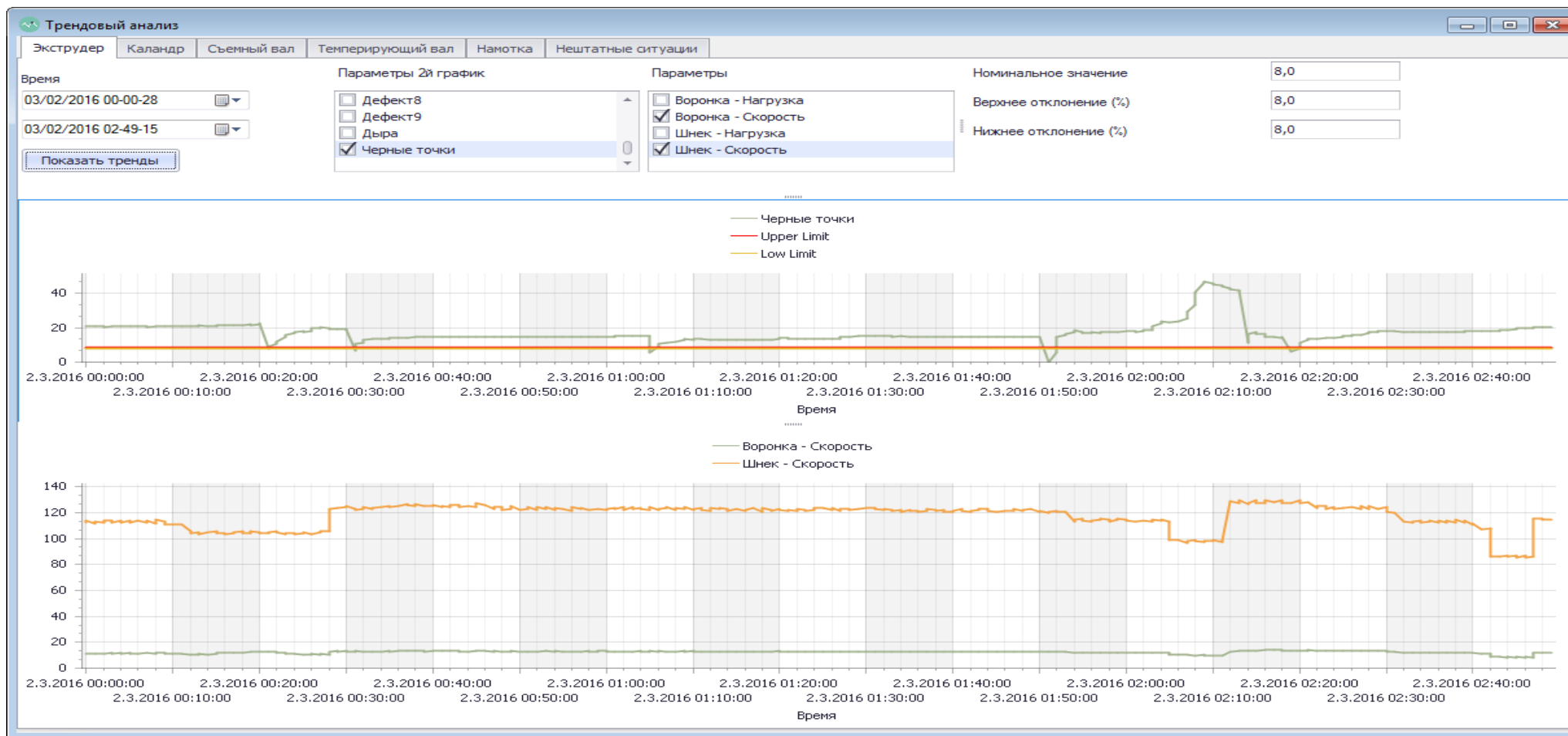


Data Mining and processing of quality data, process data and material data for the purpose of determining the causes of film failure!

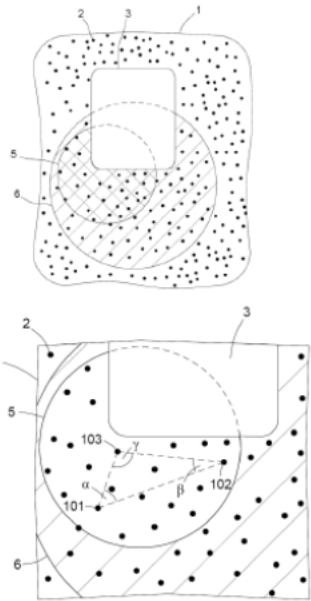
Advantage:

- SPC
- Reduce of claim
- More good production

6. small number of films errors



7. Anticounterfeiting

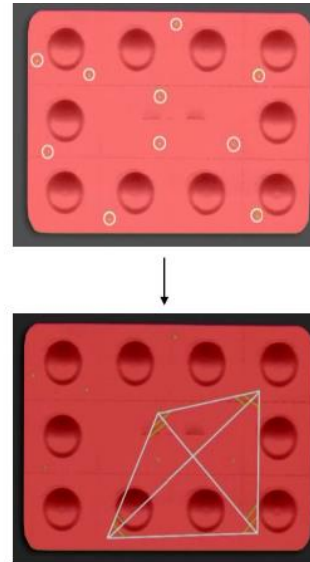
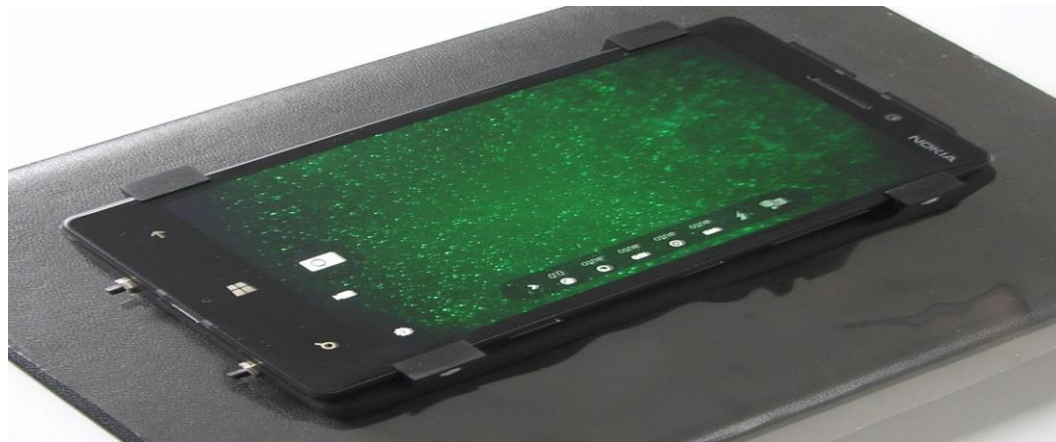


kp produces films with IR and UV pigments
0.001% (costs less than 0.01 C / m²)

- User receives an image with 3.4 or 5 points
- The software determines the angle of 1.4 or 10 triangles
- The check is to compare the angle of the existing triangles

This version is completely anti-counterfeit, since it is based on a random distribution of points!

kp-Patent: DE 10 2008 032 781 A1
WO 2010/003585 A1
vom 14.01.2010



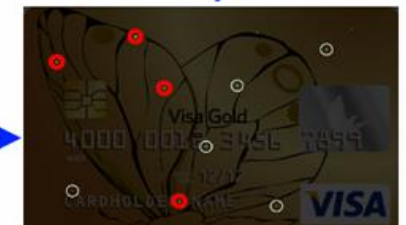
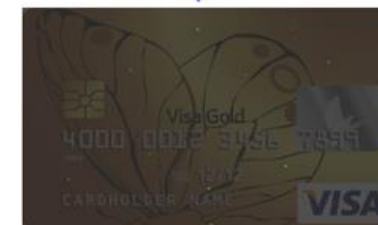
Identification data											
Card num	4000 0012 3456 7899										
Triangle 1	Triangle 2		Triangle 3			Triangle 4					
α_1	β_1	γ_1	α_2	β_2	γ_2	α_3	β_3	γ_3	α_4	β_4	γ_4
7	13	160	26	68	94	32	48	100	33	35	112
Valid thru	12.2012										
Type	Verpackung/ Kreditkarte										

Different points in a pharma blister



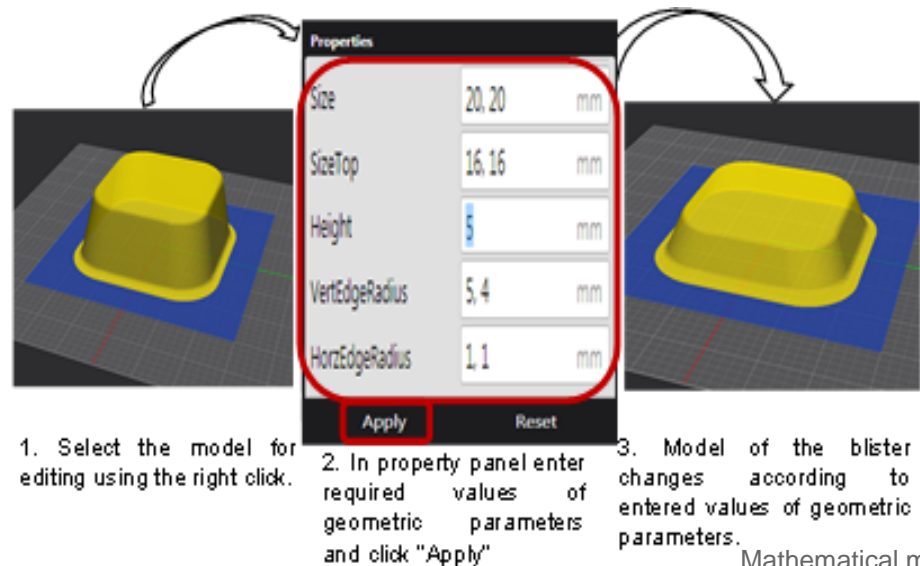
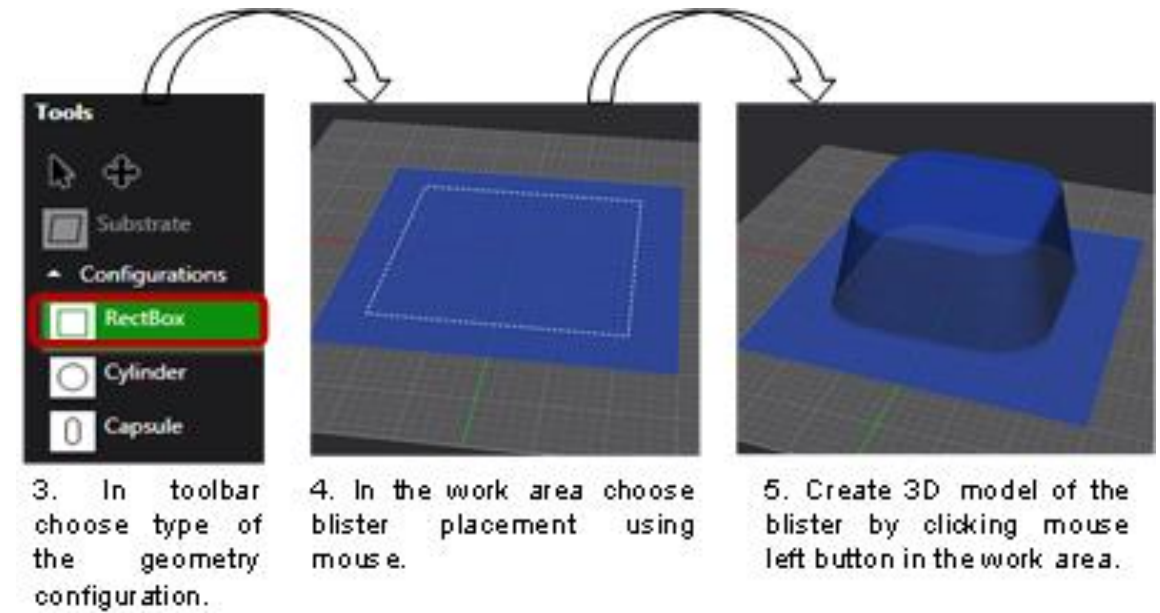
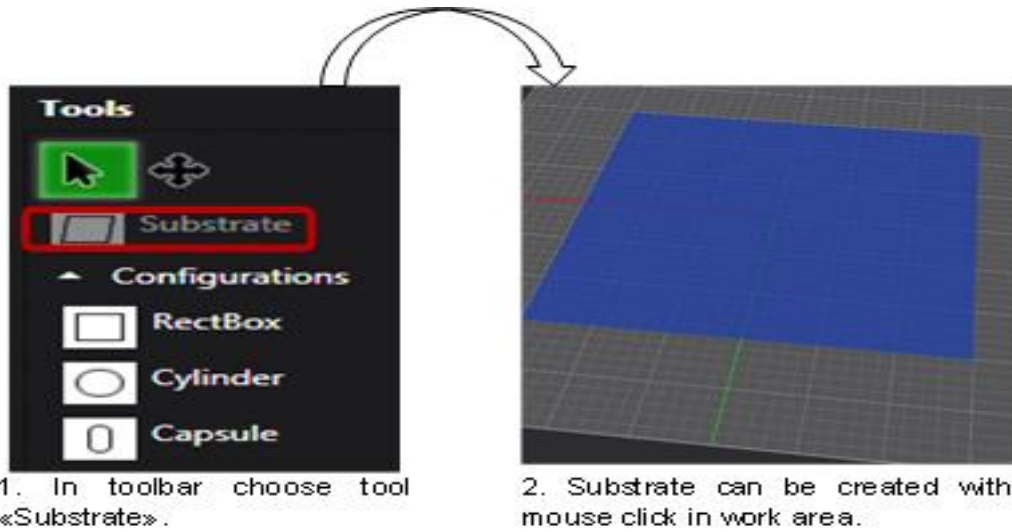
Illumination

Calculation



Separation

8. Thermoforming process



Advantage:

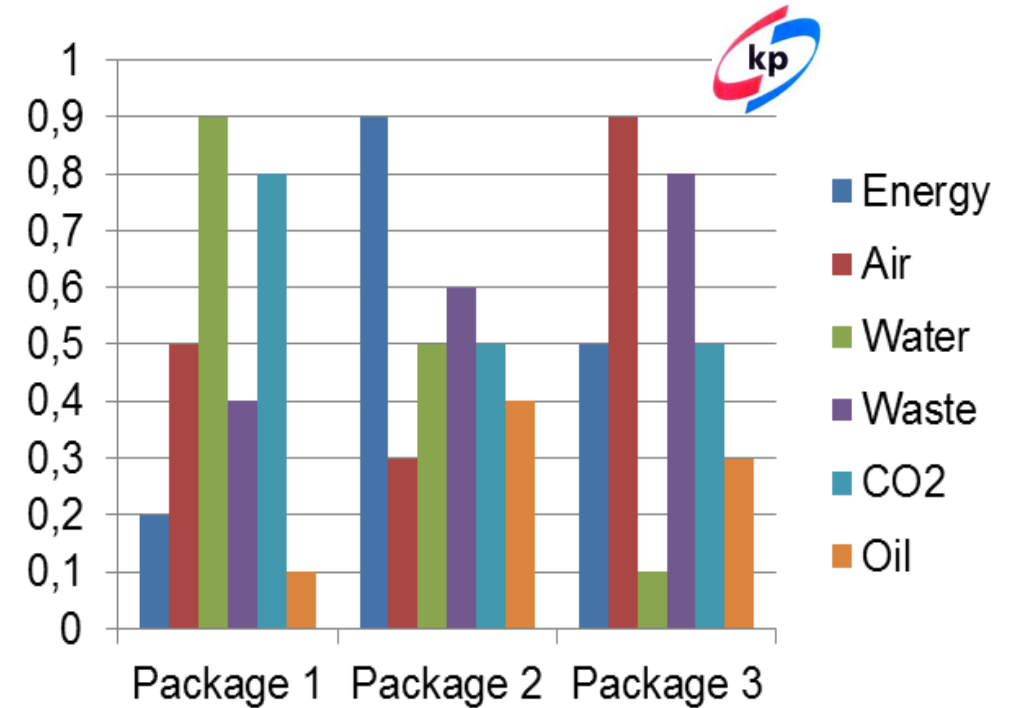
- Optimize wall thickness distribution
- Even for high barrier
- high strength

9. Ecological properties of different polymeric films

Oekobil 4 is a kp internal software which was developed by TU St.Petersburg to show the ecological comparison of different packaging material

Goal of Oekobil 4 is comparing the ecological characteristics of:

- PS
 - PET
 - PVC
 - PP
 - HDPE
 - LDPE
 - PVdC
 - PLA
 - CaCO₃
 - tin plate
 - glass
 - aluminum
 - paper
 - carton
- Energy consumption (MJ/kg)
- Air quantity (m³/kg)
- Water quantity (dm³/kg)
- Solid waste (cm³/kg)
- CO₂ emissions (mg/kg)
- Oil consumption (g/kg)
- Water consumption (l/kg)



$$\text{Eco Index Packaging 1} = (\text{Energy cons.} / \text{total energy cons.}) * 30\% + (\text{Air cons.} / \text{total air cons.}) * 20\% \dots + (\text{oil cons.} / \text{total oil cons.}) * 5\% + \dots$$

9. Ecological properties of different polymeric films

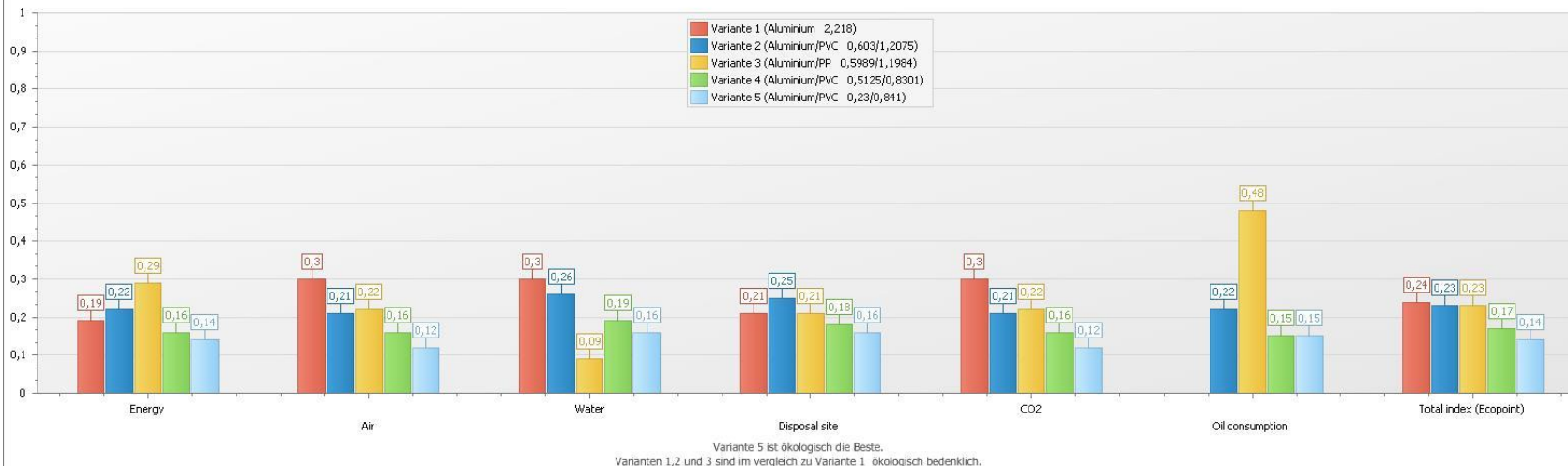


Packaging	Aluminum	PVC, aluminum	PP, aluminum	PVC, aluminum	PVC, paper, aluminum
Capacity (pieces)	10	10	10	10	10
Bottom film (gramms)	Aluminum 1,3262	PVC 1,2075	PP 1,1984	PVC 0,8301	PVC 0,841
Top film (gramms)	Aluminum 0,8922	Aluminum 0,603	Aluminum 0,5989	Aluminum 0,5125	Paper, aluminum 0,23

Ecobalances of different packages
Calculation of ecological characteristics comparable packaging:
PVC, PP, PS, HIPS, LDPE, HDPE, PET, glas, aluminium, cardboard, paper, metal (tin), etc.
Attention!
Comparison in the "OekoBilZ" program is applicable only for packages with the same contents, same volume, and same package-objective.
At the packages comparison the following deviations of the Total index (Ecopoint) are not considerable:
- 2 packages: 20%;
- 3 packages: 10%;
- 4 packages: 5%.
This rule is based on the approximate calculation method of the "OekoBilZ" program.
For all the questions regarding the method of eco-balancing, please contact:
Prof. Dr. Christian Kohlert
D-56401 Montabaur, PSF 1165
Tel.: (02602) 915357
Email: C.Kohlert@kpfilms.com

Start window
Exit from "OekoBilZ"
Start working with "OekoBilZ"

Comparison of ecological parameters for "Tablettenblister"



Advantage:

- Review environmental impact of different packaging options
- Decision support for customer

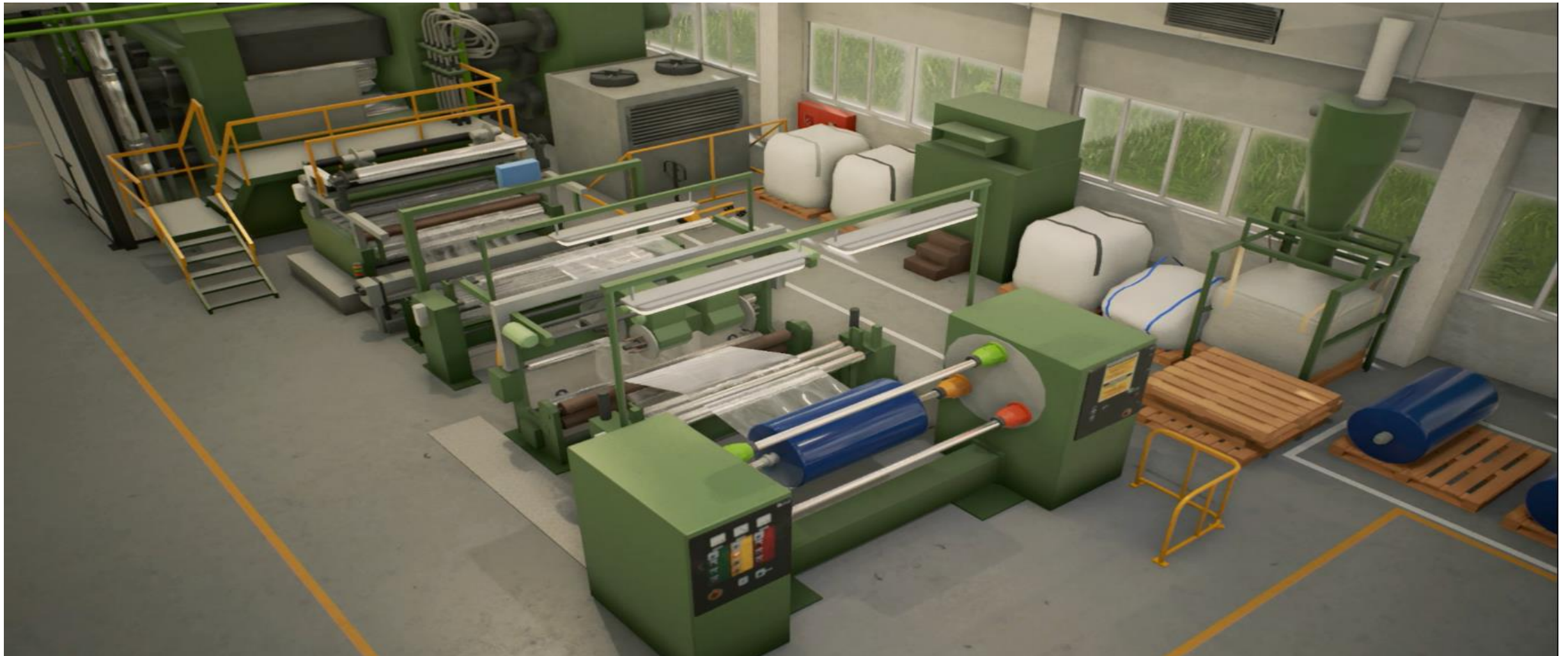
10. Plant development



Advantage:

- Optimization of machine installation in existing premises
- Optimization of process sequences
- Marketing





Future Film Center St.Petersburg

Name: Center Polymeric Engineering

machine	4-L pilot calender with PE lamination
	Laboratory mill with adhesion measurement
	Laboratory hot mixers
	2 screw laboratory extruder
	Laboratory Co-kneader BUSS
	Laboratory stretching traversal system TDO
	Laboratory stretching longitudinal system MDO
	Laboratory coating machine for nanosol
	Felt nozzle coating line
	Rotation coating line Weko
	Corona equipment
	IR and hot air drying
	IR-drying
	UV-drying
	Laboratory thermoforming machine

measurement	Oven Mathis for stability measurement
	Spectrophotometer for Lab-measurement
	Surface tension meter Krüss
	Surface friction measurement device
	surface defect camera
	Shrinkage measurement
	Shrinkage force measurement
	Hand rakel coater
	diving coater
	film thickness distribution
	format measurement
	color adhesion measurement

Type of cooperation	Contract research
	Pattern production
	Innovation processing
	Market analyse
	Literature and patent research
	further education



Possible F / E topics	development of formulation for rigid/soft films
	Technological optimization
	- compounding
	- calendaring
	- extrusion
	- lamination
	- coating
	- thermoforming
	Quality measurement with assessment
	- thickness of film
	- film defect
	- surface tension
	- color constantly
	- shrinkage and shrinkage force
	Coating with nanosol for
	- electrical surface conductivity
	- antimicrobial
	- Improvement / deterioration Printability
	- increase scratch resistance
	market analyse for polymeric products
Joint innovations - example	
- anticounterfeiting	
- flexible solar cells	
- electronic film	
- energy efficiency	
- coating of nanosol	
- using of liquid colors	



CONCEPT

SUCCESS!!

Teamwork

Prof. Dr. Christian Kohlert
Kohlert-Consulting

Danke !



Спасибо !

Innovation

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